

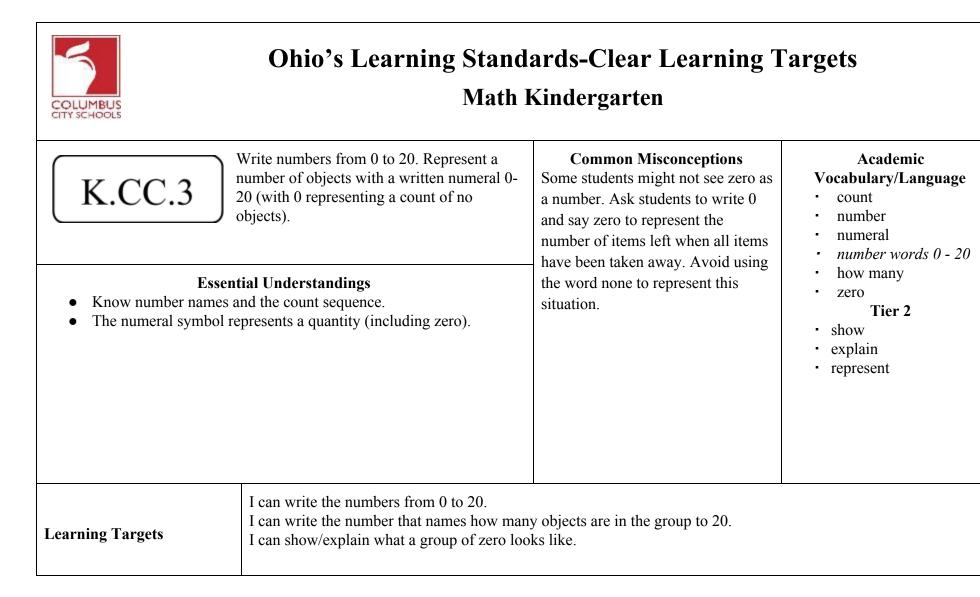
Count to 100 by ones and by tens. K.CC.1 Essential Understandings • Know number names and the count sequence. • Know there is a standard order to counting.	Common Misconceptions Because of the lack of patterns in the numbers one through twelve, some students struggle when they get to the "teen" numbers. Students will say things such as "three-teen" for thirteenth. Counting out loud often with students helps them develop the sequence for the words and see the patterns in the numbers. Use books, songs and counting chants to help the development of counting skills.	Academic Vocabulary/Language count number number words 1 - 20 ones tens
I can count to 100 by ones starting at 1I can count to 100 by tens starting at 10.		

Classroom Snapshot			
Examples "1, 2, 3, 4,"	Questions Ask students to count to 100 by ones.		
"10, 20, 30, 40," Adapted from Darke County Schools			
Ohio Department of Education Model Curriculum Instructional Strategies and Resources Students view counting as a mechanism used to land on a number. Young students mimic counting often with initial lack of purpose or meaning. Coordinating the number words, touching or moving objects in a one-to-one correspondence may be little more than a matching activity. However, saying number words as a chant or a rote procedure plays a part in students constructing meaning for the conceptual idea of counting. They will learn how to count before they understand cardinality, i.e. that the last count word is the amount of the set. Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015			
Connections Across Standards Apply counting to addition and subtraction (K.OA.1-2, 5).			
Pre K (Prior Grade Standard) Count to 20 by ones with increasing accuracy.	1.NBT.1 (Future Grade Standard) Count to 120, starting at any number less than 120. In this range, read and write numerals and represent a number of objects with a written numeral.		



K.CC.2	-	Common Misconceptions Some students might not see that you can start counting at any number. By having students count beginning at any number they develop the understanding of counting and make connections with counting patterns.	Academic Vocabulary/Language count number forward
Learning Target	I can count forward starting at any number the	hat is given to me from 1 to 100.	

Classroom Snapshot Example **Ouestions** When given a random number, Generate a random number they can count for at least 10 more. and have the student start counting from that number on. Adapted from Darke County Schools **Ohio Department of Education Model Curriculum Instructional Strategies and Resources** Counting on or counting from a given number conflicts with the learned strategy of counting from the beginning. In order to be successful in counting on, students must understand cardinality. Students often merge or separate two groups of objects and then recount from the beginning to determine the final number of objects represented. For these students, counting is still a rote skill or the benefits of counting on have not been realized. Games that require students to add on to a previous count to reach a goal number encourage developing this concept. Frequent and brief opportunities utilizing counting on and counting back are recommended. These concepts emerge over time and cannot be forced. Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015 **Connections Across Standards** Apply counting to addition and subtraction (K.OA.1-2, 5). **Pre-K (Prior Grade Standard) 1.NBT.1(Future Grade Standard)** Count to 20 by ones with increasing accuracy. Count to 120, starting at any number less than 120. In this range, read and write numerals and represent a number of objects with a written numeral.



Classroom Snapshot		
Examples	Questions	
1,2,3, 20	Write the numerals from 1 - 20.	
$\star \star \star \star \star$ is 4	Write the number of bear counters on the table.	
"A group of zero has no objects."	Explain why this group has zero blocks.	
Adapted from Darke County Schools		

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Like counting to 100 by either ones or tens, writing numbers from 0 to 20 is a rote process. Initially, students mimic the actual formation of the written numerals while also assigning it a name. Over time, children create the understanding that number symbols signify the meaning of counting. Numerals are used to communicate across cultures and through time a certain meaning. Numbers have meaning when children can see mental images of the number symbols and use those images with which to think. Practice count words and written numerals paired with pictures, representations of objects, and objects that represent quantities within the context of life experiences for kindergarteners. For example, dot cards, dominoes and number cubes all create different mental images for relating quantity to number words and numerals. One way students can learn the left to right orientation of numbers is to use a finger to write numbers in air (skywriting). Children will see mathematics as something that is alive and that they are involved. Students should study and write numbers 0 to 20 in this order: numbers 1 to 9, the number 0, then numbers 10 to 20. They need to know that 0 is the number items left after all items in a set are taken away. Do not accept "none" as the answer to "How many items are left?" for this situation.

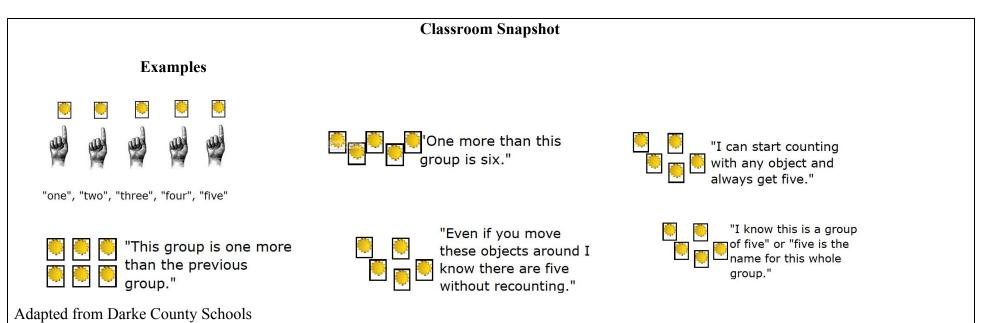
Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards Apply to the teen numbers (K.NBT.1).

Pre-K (Prior Grade Standard)	1.NBT.1 (Future Grade Standard)	
Identify and name numerals 1-9.	Count to 120, starting at any number less than 120. In this range, read	
	and write numerals and represent a number of objects with a written	
	numeral.	



 K.CC.4 a. When counting objects, estal number names in the standard one number name and each number of the order in which is understand that the last number of the order in which is understand that the number of arrangement or the order in which is understand that each success one larger. Essent A one-to-one relationsh name and one numeral. Each counted number stated 	sive number name refers to a quantity that is tial Understandings hip connects one object with one number	Common Misconceptions Some students might think that the count word used to tag an item is permanently connected to that item. So when the item is used again for counting and should be tagged with a different count word, the student uses the original count word. For example, a student counts four geometric figures: triangle, square, circle and rectangle with the count words: one, two, three, four. If these items are rearranged as rectangle, triangle, circle and square and counted, the student says these count words: four, one, three, two.	Academic Vocabulary/Language number number words 0 - 20 Tier 2 count name find
Learning Targets	I can count objects by touching and saying the correct number for each object. I can name the number of objects in a group after counting. I know the number of objects in a group does not change even when I start counting with a different object. I can name the number of objects in a group even after they have been mixed up. I can make a set that is one more than than a given number.		



Ohio Department of Education Model Curriculum Instructional Strategies and Resources

One of the first major concepts in a student's mathematical development is cardinality. Cardinality, knowing that the number word said tells the quantity you have and that the number you end on when counting represents the entire amount counted. The big idea is that number means amount and, no matter how you arrange and rearrange the items, the amount is the same. Until this concept is developed, counting is merely a routine procedure done when a number is needed. To determine if students have the cardinality rule, listen to their responses when you discuss counting tasks with them. For example, ask, "How many are here?" The student counts correctly and says that there are seven. Then ask, "Are there seven?" Students may count or hesitate if they have not developed cardinality. Students with cardinality may emphasize the last count or explain that there are seven because they counted them. These students can now use counting to find a matching set.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards Count a collection by ones (K.CC.1). Count a collection of pennies (K.MD.3).	
Pre-K (Prior Grade Standard) Demonstrate one-to-one correspondence when counting objects up to 10.	1.NBT.1 (Future Grade Standard) Count to 120, starting at any number less than 120. In this range, read and write numerals and represent a number of objects with a written numeral.



K.CC.5 in configuration; given a number Essent • Count to tell the number	bes not change based on the arrangement,	Common Misconceptions Some students might think that the count word used to tag an item is permanently connected to that item. So when the item is used again for counting and should be tagged with a different count word, the student uses the original count word. For example, a student counts four geometric figures: triangle, square, circle and rectangle with the count words: one, two, three, four. If these items are rearranged as rectangle, triangle, circle and square and counted, the student says these count words: four, one, three, two.	Academic Vocabulary/Language count number number words 0 - 20
Learning Targets	I can count a set of objects up to 20 in an org I can count a set of objects up to 10 that are I can count out the correct number of objects	in a scattered arrangement.	

Examples

When you drop a group of 7 objects on the table, they can count then and tell you how many.

When you arrange 15 objects in 5 rows of three, the student can count then.

"If you tell me to make a group of 16, I can select counters and make that group.

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students develop the understanding of counting and cardinality from experience. Almost any activity or game that engages children in counting and comparing quantities, such as board games, will encourage the development of cardinality. Frequent opportunities to use and discuss counting as a means of solving problems relevant to kindergarteners is more beneficial than repeating the same routine day after day. For example, ask students questions that can be answered by counting up to 20 items in multiple situations.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards Count a collection by ones (K.CC.1). Count a collection of pennies (K.MD.3).	
Pre-K (Prior Grade Standard) Understand that the last number spoken tells the number of objects counted.	1.NBT.1 (Future Grade Standard) Count to 120, starting at any number less than 120. In this range, read and write numerals and represent a number of objects with a written numeral.

Questions

Count this group of counters. How many counters are there?

They can count organized counters that are "arranged" in groups up to 20.

Given a random number from 1 to 20, they can assemble that many counters.



K.CC.6 symbols one get than, another group, not to exceed 10 ob Essential U • The terms greater/more that used when comparing object	Understandings In, less/fewer than, and same as can be cts and numerals. not change based on the arrangement,	Common Misconceptions Students may look at objects and focus on their size, arrangement, or area when making comparisons between groups and not the number.	Academic Vocabulary/Language - equal to - same as - greater than - more than - less than - fewer than Tier 2 - identity - compare
Learning Target I ca	an compare two groups and tell which has	the greater number, which has lesser n	umber, or if they are the same.

Classroon	ı Snapshot
ExampleQuestion"When I see a group of 7, I can tellCompare these two groups anyou which groups is greater (or fewer)which one is greater (or fewer)by counting or sometimes by justthe same.looking at the arrangement."the same.	
Adapted from Darke County Schools Ohio Department of Education Model Curriculum Instructional Stra As children develop meaning for numerals, they also compare these nume differences in these different representations. They can use strategies such same as another group.	erals to the quantities represented. Children can look for similarities and as matching or counting to determine which group is more, less, or the
Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2 Connections Across Standards Count to determine the number of objects (K.CC.4-5). Count the number in each category (K.MD.3). Compare two objects to see which object has "more of" or "less of" a unit	
Pre-K (Prior Grade Standard) Identify whether the number of objects in one group is greater than, less than or equal to the number of objects in another group up to 10.	1.NBT.3 (Future Grade Standard) Compare two two-digit numbers based on meanings of the tens and ones digits, recording the results of comparisons with the symbols >, =, and <.



K.CC.7 Compare (without using inequality symbols) two numbers between 0 and 10 when presented as written numerals. Essential Understanding • Compare numbers.	Common Misconceptions Students possibly have misconceptions about comparing the numbers between 1 and 10 when only using written numerals because the numeral is an abstract representation of a quantity. Students must have mastery of the concrete representations of written numerals and quantities long before they would be asked to compare the written numerals alone. Adapted from Homestead County	Academic Vocabulary/Language - more - less - greater than - more than - less than - fewer than Tier 2 - compare - tell
Learning Target I can look at two numbers from 1 to 10 and t	tell which is greater than, less than, mor	re than or fewer than.

Example "I know that '7' is larger than '5' and even better I know it is '2' larger."

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Students need to explain their reasoning when they determine whether a number is greater than, less than, or equal to another number. Teachers need to ask probing questions such as "How do you know?" to elicit their thinking. For students, these comparisons increase in difficulty, from greater than to less than to equal.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards

Count to determine the number of objects (K.CC.4-5).

Count the number in each category (K.MD.3)

Count two objects to see which object has "more of" or "less of" a unit (K.MD.2)

Pre-K (Prior Grade Standard)	1.NBT.3 (Future Grade Standard)
Identify whether the number of objects in one group is greater than, less than or equal to the number of objects in another group up to 10.	Compare two two-digit numbers based on meanings of the tens and ones digits, recording the results of comparisons with the symbols >,
than of equal to the number of objects in another group up to 10.	=, and <.

Question Compare two numbers and tell which is greater than or less than.



 K.OA.1 Represent addition and subtraction with objects, fingers, mental images, drawings, sounds such as claps, acting out situations, verbal explanations, expressions, or equations. Drawings need not show details, but should show the mathematics in the problem. (This applies wherever drawings are mentioned in the Standards.) Essential Understandings Addition is putting together. Subtraction is taking apart, taking from, or comparing two quantities. There is a relationship between addition and subtraction. Adding 1 results in the next number in a counting sequence. Subtracting 1 results in the previous number in a counting sequence. O is the number of items left when all the objects in a set are taken away. 	Common Misconceptions Students may over-generalize the vocabulary in word problems and think that certain words indicate solution strategies that must be used to find an answer. They might think that the word more always means to add and the words take away or left always means to subtract. When students use the words take away to refer to subtraction and its symbol, teachers need to repeat students' ideas using the words minus or subtract. For example, students use addition to solve this problem: Seth took the 4 stickers he no longer wanted and gave them to Anna. Now Seth has 5 stickers left. How many stickers did Seth have to begin with?	Academic Vocabulary/Language - add - subtract - putting together - adding to - taking apart - taking from Tier 2 - show - model - draw - act out
Learning TargetsI can add in many ways (including objects, I can subtract in many ways (including objects)		

Classroom	Snapshot
-----------	----------

Examples
"I can show $2 + 3$ by putting counters
out and showing the total of 5"

"I can show 7-4 by having 7 students stand in a group and then have 4 students walk away"

Adapted from Darke County Schools

Questions Show 3 + 5 two different ways.

Model 7 - 2 two different ways

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Provide contextual situations for addition and subtraction that relate to the everyday lives of kindergarteners. A variety of situations can be found in children's literature books. Students then model the addition and subtraction using a variety of representations such as drawings, sounds, acting out situations, verbal explanations and numerical expressions. Manipulatives, like two-color counters, clothespins on hangers, connecting cubes and stickers can also be used for modeling these operations.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015		
Connections Across Standards		
Write numerals in mathematical representations (K.CC.3).		
Use counting and cardinality to represent addition and subtraction (K.CC.4-5).		
Count the number of objects in each category (K.MD.3).		
Pre-K Prior Grade Standard)	1.OA.1 (Future Grade Standard)	
Count to solve simple addition and subtraction problems with totals	Use addition and subtraction within 20 to solve word problems	
smaller than 8, using concrete objects. involving situations of adding to, taking from, putting together, tak		
	apart and comparing, with unknowns in all positions, e.g., by using	
	objects, drawings, and equations with a symbol for the unknown	
	number to represent the problem. See Table 1, page 95.	



 K.OA.2 Solve addition and subtraction problems (written or oral), and add and subtract within 10 by using objects or drawings to represent the problem. Essential Understandings Addition is putting together. Subtraction is taking apart, taking from, or comparing two quantities. There is a relationship between addition and subtraction. There are different problems types: add to (result unknown); take from (results unknown); and put together/take apart (total unknown and both addends unknown) (See Glossary Table 1; page 95) 	Common Misconceptions Students may over-generalize the vocabulary in word problems and think that certain words indicate solution strategies that must be used to find an answer. They might think that the word more always means to add and the words take away or left always means to subtract. When students use the words take away to refer to subtraction and its symbol, teachers need to repeat students' ideas using the words minus or subtract. For example, students use addition to solve this problem: Seth took the 4 stickers he no longer wanted and gave them to Anna. Now Seth has 5 stickers left. How many stickers did Seth have to begin with?	Academic Vocabulary/Language - add - in all - join - are left - subtract - minus Tier 2 - solve - use
Learning TargetI can solve problems using addition and sub I can explain my thinking.	otraction.	

Example

The student can consistently solve addition and subtraction word problems.

Question "Billy has 6 hats and Sally has 4 hats. Who has more? How many more?"

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Provide contextual situations for addition and subtraction that relate to the everyday lives of kindergarteners. A variety of situations can be found in children's literature books. Students then model the addition and subtraction using a variety of representations such as drawings, sounds, acting out situations, verbal explanations and numerical expressions. Manipulatives, like two-color counters, clothespins on hangers, connecting cubes and stickers can also be used for modeling these operations.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

	RESULT UNKNOWN	CHANGE UNKNOWN	START UNKNOWN	
ADD TO	Two bunnies sat on the grass. Three more bunnies hopped there. How many bunnies are on the grass now? 2 + 3 = ?	Two bunnies were sitting on the grass. Some bunnies hopped there. Then there were five bunnies. How many bunnies hopped over to t first two?	more bunnies hopped there. Then there were	
	2.0.1	2 + ? = 5	? + 3 = 5	
TAKE FROM	Five apples were on the table. I ate two apples. How many apples are on the table now? 5-2=?	Five apples were on the table. I ate some app Then there were three apples. How many app did I eat?		
		5 - ? = 3	? - 2 = 3	
	TOTAL UNKNOWN	ADDEND UNKNOWN	BOTH ADDENDS UNKNOWN ¹	
PULL TOGETHER/	Three red apples and two green apples are on the table. How many apples are on the table?	Five apples are on the table. Three are red ar rest are green. How many apples are green?	d the Grandma has five flowers. How many can she put in her red vase and how many in her blue vase?	
TAKE APART ²	3 + 2 = ?	3 + ? = 5, 5 - 3 = ?	5 = 0 + 5, 5 = 5 + 0	
			5 = 1 + 4, 5 = 4 + 1	
			5 = 2 + 3, 5 = 3 + 2	
	DIFFERENCE UNKNOWN	BIGGER UNKNOWN	SMALLER UNKNOWN	
COMPARE ³	("How many more?" version): Lucy has two apples. Julie has five apples. How many more apples does Julie have than Lucy? ("How many fewer?" version): Lucy has two apples. Julie has five apples. How many fewer apples does Lucy have	(Version with "more"): Julie has three more as than Lucy. Lucy has two apples. How many a does Julie have? (Version with "fewer"): Lucy 3 fewer apples than Julie. Lucy has two apple How many apples does Julie have?	boles than Lucy. Julie has five apples. How many apples does Lucy have? (Version with "fewer"): Lucy has	
	than Julie?	2 + 3 = ?, 3 + 2 = ?	5 - 3 = ?, ? + 3 = 5	
	2 + ? = 5, 5 - 2 = ?			
he = sign does not nnections rite numera e counting	situations can be used to show all the decompositions of a give always mean "makes" or "results in" but always does mean "i Across Standards als in mathematical representations (and cardinality to represent addition mber of objects in each category (K	(K.CC.3). n and subtraction (K.CC.4-5).	e total on the left of the equal sign, help children understand that	
. V (Duise	Cuada Standard)	1.0	A 1 (Entrue Cuado Stondard)	
	· Grade Standard)	1.OA.1 (Future Grade Standard)		
haller than 8, using concrete objects. in a o		Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, takin apart and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem. See Table 1, page 95.		



K.OA.3 Decompose numbers and record compositions for numbers less than or equal to 10 into pairs in more than one way by using objects and, when appropriate, drawings or equations. Essential Understanding • There is more than one way to compose or decompose a number.	Common Misconceptions Students often do not realize that there are many different ways to break a number down in to parts. By giving students manipulatives, they can explore the different ways to make a number. Once students are successful using the manipulatives, they can move to pictorial and then numerical representations.	Academic Vocabulary/Language - add - in all - join - are left - subtract - minus - plus sign + - minus sign - - equals sign = - break apart - put together - equation Tier 2 - decompose - record
Learning Target I can break apart a number from 1 to 10 and	show it in different ways.	

Classroom Snapshot				
ExampleQuestion"Seven can be 3 and 4,Show as many ways as you can to 15 and 2, 4 and 2, 2 and 5,the number 7?6 and 1, 7 and 0"5				
Adapted from Darke County Schools Ohio Department of Education Model Curriculum Instructional Strategies and Resources Have students decompose numbers less than or equal to 5 during a variety of experiences to promote their fluency with sums and differences less than or equal to 5 that result from using the numbers 0 to 5. For example, ask students to use different models to decompose 5 and record their work with drawings or equations. Next, have students decompose 6, 7, 8, 9, and 10 in a similar fashion. As they come to understand the role and meaning of arithmetic operations in number systems, students gain computational fluency, using efficient and accurate methods for computing. Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015				
Connections Across Standards Write numerals in mathematical representations (K.CC.3). Use counting and cardinality to represent addition and subtraction (K.CC.4-5). Count the number of objects in each category (K.MD.3).				
Pre-K (Prior Grade Standard) Count to solve simple addition and subtraction problems with totals smaller than 8, using concrete objects.	1.OA.3 (Future Grade Standard) Apply properties of operations as strategies to add and subtract. For example, if $8 + 3 = 11$ is known, then $3 + 8 = 11$ is also known (Commutative Property of Addition); to add $2 + 6 + 4$, the second two numbers can be added to make a ten, so $2 + 6 + 4 = 2 + 10 = 12$ (Associative Property of Addition). Students need not use formal terms for these properties			

Г



KOA.4 For any number from 1 to 9, find the number that makes 10 when added to the given number, e.g., by using objects or drawings, and record the answer with a drawing or, when appropriate, an equation. Essential Understanding • Addition is putting together.	Common Misconceptions Students often do not realize that there are many different ways to break a number down in to parts. By giving students manipulatives, they can explore the different ways to make a number. Once students are successful using the manipulatives, they can move to pictorial and then numerical representations.	Academic Vocabulary/Language add plus sign + equals sign = ten equation Tier 2 find record
Learning Target Given a number from 1 to 9, I can find the number to make 10 and show it in different ways.		

Example

"I know if I have 7 it takes three more to make 10. I can show 7 + 3 = 10by using a ten frame chart, using groups of counters, or by drawing.

Questions

If you have 6, how many more do you need to make 10? Can you show how you know?

Delmar has 10 buttons. Some are blue and some are red. How many blue and red buttons might he have?

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Create written addition problems with sums equal to 10. It is important to use a problem context that is relevant to kindergarteners. After the teacher reads the problem, students choose their own method to model the problem and find a solution. Students discuss their solution strategies while the teacher represents the situation with an equation written under the problem. The teacher and students should use the words equal and is the same as interchangeably.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards

Write numerals in mathematical representations (K.CC.3).

Use counting and cardinality to represent addition and subtraction (K.CC.4-5).

Count the number of objects in each category (K.MD.3).

Pre-K (Prior Grade Standard)	1.OA.4 (Future Grade Standard)
Count to solve simple addition and subtraction problems with totals smaller than 8, using concrete objects.	



 Fluently ^G add and subtract within 5. K.OA.5 Essential Understandings There is a relationship between addition and subtraction. Adding 1 results in the next number in a counting sequence. Subtracting 1 results in the previous number in a counting sequence. Adding or subtracting 0 results in the same number. 0 is the number of items left when all the objects in a set are taken away. Fluency is the ability to use efficient, accurate, and flexible methods for computing. 	Common Misconceptions Teachers need to provide instructional experiences so that students progress from the concrete level (manipulatives), to the pictorial level, then to the abstract (expressions/equations) level when learning mathematical concepts. Students who skip pictorial thinking are more likely to use finger counting and rote memorization for work with addition and subtraction.	Academic Vocabulary/Language • add • subtract
Learning Target I can easily add and subtract any of the num	nbers from 1 to 5.	

Classroo	m Snapshot
Example "I can add and subtract within 5 quickly without external help or counting in my head."	Question Add 2 + 3 without counters.
 with drawings or equations. Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum Connections Across Standards Write numerals in mathematical representations (K.CC.3). Use counting and cardinality to represent addition and subtraction. (K.CC.) 	y of experiences to promote their fluency with sums and differences less ask students to use different models to decompose 5 and record their work 2015
Count the number of objects in each category (K.MD.3). Pre-K (Prior Grade Standard) Count to solve simple addition and subtraction problems with totals smaller than 8, using concrete objects.	1.OA.6 (Future Grade Standard) Add and subtract within 20, demonstrating fluency ^G with various strategies for addition and subtraction within 10. Strategies may include counting on; making ten, e.g., $8 + 6 = 8 + 2 + 4 = 10 + 4 = 14$; decomposing a number leading to a ten, e.g., $13 - 4 = 13 - 3 - 1 = 10$ -1 = 9; using the relationship between addition and subtraction, e.g., knowing that $8 + 4 = 12$, one knows $12 - 8 = 4$; and creating equivalent but easier or known sums, e.g., adding $6 + 7$ by creating the known equivalent $6 + 6 + 1 = 12 + 1 = 13$.



KNBT.1 Compose and decompose numbers from 11 to 19 into a group of ten ones and some further ones by using objects and, when appropriate, drawings or equations; understand that these numbers are composed of a group of ten ones and one, two, three, four, five, six, seven, eight, or nine ones. Essential Understandings • Work with numbers 11–19 to gain foundations for place value. • The basic unit of the base-ten system is a one. • Teen numbers are composed of a group of ten ones and more ones. • A group of ten consists of ten "ones".	Common Misconceptions Students have difficulty with ten as a singular word that means 10 things. For many students, the understanding that a group of 10 things can be replaced by a single object and they both represent 10 is confusing. Help students develop the sense of 10 by first using groupable materials then replacing the group with an object or representing 10. Watch for and address the issue of attaching words to materials and groups without knowing what they represent. If this misconception is not addressed early on it can cause additional issues when working with numbers 11-19 and beyond.	Academic Vocabulary/Language - ten 10 - number words 11 through 19 - compose - decompose - equation - ones - tens Tier 2 - record - tell - show
Learning Target Given a number from 11 to 19, I can tell and	show how many tens and how many or	nes make the number.

Example "I know that 14 is a ten and four more. I can also show that with a ten stick and 4 additional blocks."	Question How can you make 17? Can you show that with base-ten blocks?
to construct their own base-ten ideas about quantities and their manipulatives to model and connect equivalent representations	an develop the strategy of adding onto 10 to add within 20 in Grade 1. Students need r symbols by connecting to counting by ones. They should use a variety of s for the numbers 11 to 19. For instance, to represent 13, students can count by ones oup of 5 beans and 8 beans or anchor to ten and show one group of 10 beans and 3 10 ones.
Connections Across Standards Decompose numbers (K.OA.3). Know and write numerals to 20 and count on from any given r	
Pre-K (Prior Grade Standard) N/A	1.NBT.2 (Future Grade Standard) Understand that the two digits of a two-digit number represent amounts of tens and ones. Understand the following as special cases: 10 can be thought of as a bundle of ten ones — called a "ten;" the numbers from 11 to 19 are composed of a ten and one, two, three, four, five, six, seven, eight, or nine ones; and the numbers 10, 20, 30, 40, 50, 60, 70, 80, 90 refer to one, two, three, four, five, six, seven, eight, or nine tens (and 0 ones).



K.MD.1 (length, we using voca	8	Common Misconceptions Discourage the use of the words bigger and smaller and ask the students to use words appropriate to the attributes they are measuring. For length, objects are shorter and longer, for weight heavier and lighter, and height taller and shorter. Grade K Common Core Math	Academic Vocabulary/Language height length weight shorter longer heavier lighter taller shorter Tier 2 describe compare explain
Learning Target I can describe different ways to measure an object.			

Example

"I can describe an object identifying how long, tall or heavy it is."

Questions

Ask a student to choose an object and describe it (e.g. "This block has 2 long sides and 2 shorter sides.")

Can the student describe more than one attribute? Does the student only describe length? Do they consider width or weight?

Adapted from Darke County Schools Grade K Common Core Math

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

It is critical for students to be able to identify and describe measurable attributes of objects. An object has different attributes that can be measured, like the height and weight of a can of food. When students compare shapes directly, the attribute becomes the focus. For example, when comparing the volume of two different boxes, ask students to discuss and justify their answers to these questions: Which box will hold the most? Which box will hold least? Will they hold the same amount? Students can decide to fill one box with dried beans then pour the beans into the other box to determine the answers to these questions.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards Classify objects into given categories (K.MD.3). Compare quantities of objects (K.CC.6).

Pre-K (Prior Grade Standard)	1.MD.1 (Future Grade Standard)
Sort and classify objects by one or more attributes (e.g., size, number).	Order three objects by length; compare the lengths of two objects
	indirectly by using a third object.



K.MD.2 main will atter example, directly compare the here is the child as taller/shorter. Essentian described.	irectly compare two objects with a easurable attribute in common, to see hich object has "more of" or "less of" the tribute, and describe the difference. For neights of two children and describe one al Understandings tributes that can be identified and ttributes that can be compared.	Common Misconceptions Discourage the use of the words bigger and smaller and ask the students to use words appropriate to the attributes they are measuring. For length, objects are shorter and longer and for weight heavier and lighter. Grade K Common Core Math	Academic Vocabulary/Language
Learning Target I can compare two objects by measurement and talk about how they are different.			

Example

"I know when comparing two books that one might be longer or wider and also it could be heavier."

Question Circle the object that is lighter



Adapted from Darke County Schools Grade K Common Core Math

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Have students work in pairs to compare their arm spans. As they stand back-to-back with outstretched arms, compare the lengths of their spans, then determine who has the smallest arm span. Ask students to explain their reasoning. Then ask students to suggest other measurable attributes of their bodies that they could directly compare, such as their height or the length of their feet.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards Classify objects into given categories (K.MD.3). Compare quantities of objects (K.CC.6).

Pre-K(Prior Grade Standard)	1.MD.2 (Future Grade Standard)
Describe and compare objects using measurable attributes (e.g., length, size, capacity and weight).	Express the length of an object as a whole number of length units, by laying multiple copies of a shorter object (the length unit) end to end; understand that the length measurement of an object is the number of same-size length units that span it with no gaps or overlaps. <i>Limit to contexts where the object being measured is spanned by a</i> <i>whole number of length units with no gaps or overlaps.</i>



K.MD.3 or equal to ten. Counting and so Essent • Groups of objects can b • Classifying objects is the and naming those categories	lassify objects into given categories; count in numbers of objects in each category and out the categories by count. The number of bjects in each category should be less than orting coins should be limited to pennies. ial Understandings be classified in multiple ways and counted. The process of sorting objects into categories gories. a manipulative to count and sort.	Common Misconceptions During initial instruction, students may need guidance in identifying the categories in which to sort objects. Grade K Common Core Math	Academic Vocabulary/Language - alike - different - shape - size - sort - count Tier 2 - classify - category - categorize
Learning Targets I can put objects into groups so that each group has something the same. I can count the objects in a group and put the groups in order from least to greatest.			

Examples

"Given some shapes I can sort then into groups by color or shape."

"I counted the shapes in each group and can arrange them from the largest group and the smallest".

Questions

Show the student's a collections of cubes. Say: "I have a set of cubes. Sort these cubes by color."

After the students have sorted the cubes by color, say : *Count the number of cubes in each group. How many cubes do you have in each group? Do you have any groups that have the same amount? "* Prompt if needed: *"Which groups have the same amount?"*

Adapted from Darke County Schools Grade K Common Core Math

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Provide categories for students to use to sort a collection of objects. Each category can relate to only one attribute, like Red and Not Red or Hexagon and Not Hexagon, and contain up to 10 objects. Students count how many objects are in each category and then order the categories by the number of objects they contain.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards

Count to answer "how many?" questions (K.CC.5).

Identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group (K.CC.6). Compare two numbers between 1 and 10 represented as written numerals (K.CC.7).

Pre-K (Prior Grade Standard)	1.MD.4 (Future Grade Standard)
Sort and classify objects by one or more attributes (e.g., size, number).	Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.



K.G.1 Describe objects in the environment using names of shapes, and describe the relative positions of these objects using terms such as <i>above, below, beside, in front of, behind, and next to.</i> Essential Understandings • Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinders, and spheres). • Shapes exist in the environment. • Shapes can be described by position and location.	Common Misconceptions Students many times use incorrect terminology when describing shapes. For example students may say a cube is a square or that a sphere is a circle. The use of the two-dimensional shape that appears to be part of a three-dimensional shape to name the three-dimensional shape is a common misconception. Work with students to help them understand that the two-dimensional shape is a part of the object but it has a different name.	Academic Vocabulary/Language above below in front of behind beside next to square circle triangle rectangle hexagon cube cone cylinder sphere
		Tier 2 describe find identify location
Learning Targets I can find and name shapes that I find all around me. I can describe the location of shapes I find around me.		

Classroom Snapshot		
Examples "I can find many 'triangles' in the classroom."	Questions Point to a rectangle in the classroom.	
"I can tell my friends there is a square above their head on the ceiling."		
Adapted from Darke County Schools Grade K Common Core Math Ohio Department of Education Model Curriculum Instructional Strategies and Resources Ask students to find rectangles in the classroom and describe the relative positions of the rectangles they see, e.g. This rectangle (a poster) is over the sphere (globe). Teachers can use a digital camera to record these relationships. Hide shapes around the room. Have students say where they found the shape using positional words, e.g. I found a triangle UNDER the chair. Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015 Connections Across Standards Identify and describe measurable attributes (K.MD.1). Directly compare two objects with a measurable attribute (K.MD.2).		
Pre-K(Prior Grade Standard) Demonstrate understanding of the relative position of objects using terms such as in/on/under, up/down, inside/outside, above/ below, beside/between, in front of/ behind and next to.	1.G.1 (Future Grade Standard) Distinguish between defining attributes (e.g., triangles are closed and three-sided) versus non-defining attributes (e.g., color, orientation, overall size); build and draw shapes to possess defining attributes.	



 K.G.2 Correctly name shapes regardless of orientations or overall size. Essential Understandings Identify and describe shapes (squares, circles, triangles, r hexagons, cubes, cones, cylinders, and spheres). Shapes can be identified regardless of size or orientation. 	Students many times use incorrect terminology when describing shapes. For example students may say a cube is a square or that a sphere is a circle. The use of the two-dimensional shape that appears to be part of a three-dimensional shape to name the	Academic Vocabulary/Language - circle - rectangle - hexagon - triangle - square - cube - cone - cylinder - sphere - straight - round - side - vertex - shapes - solids Tier 2 - name - identify - describe
Loowning Lowgots	n after they have been moved around (rotated, flipped, e ven after they have been moved around (rotated, flipped,	,

Examples "I know a square no matter how you turn it or color it."	Questions Show the students a triangle. Ask: <i>What is name of this shape? How do you know that this is a triangle?</i> Rotate the shape and repeat the questions.	
"I know a cylinder no matter how you turn it or color it."	Show the students a cube. Ask: <i>What is the name of this solid?" How do you know that this is a cube?</i> Show them a different size cube and repeat the questions.	
Adapted from Darke County Schools Grade K Common Core Math Ohio Department of Education Model Curriculum Instructional Stratus Use a shape in different orientations and sizes along with non-examples of shape. Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum	of the shape so students can learn to focus on defining attributes of the	
Connections Across Standards Identify and describe measurable attributes (K.MD. 1). Directly compare two objects with a measurable attribute (K.MD.2). Classify objects into given categories (K.MD.3).		
Pre-K(Prior Grade Standard) Understand and use names of shapes when identifying objects.	1.G.1 (Future Grade Standard) Distinguish between defining attributes (e.g., triangles are closed and three-sided) versus non-defining attributes (e.g., color, orientation, overall size); build and draw shapes to possess defining attributes.	



K.G.3 Identify shapes as two-dimensional (lying in a plane, "flat") or three-dimensional ("solid"). Essential Understandings • Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinders, and spheres). • Shapes can be categorized as two-dimensional (flat) or three-dimensional (solid).	Common Misconceptions Students many times use incorrect terminology when describing shapes. For example students may say a cube is a square or that a sphere is a circle. The use of the two-dimensional shape that appears to be part of a three-dimensional shape to name the three-dimensional shape is a common misconception. Work with students to help them understand that the two-dimensional shape is a part of the object but it has a different name.	Academic Vocabulary/Language circle rectangle hexagon triangle square cube cylinder cone sphere two-dimensional three-dimensional shapes solids Tier 2 name label
Learning TargetsI can name 2-D (flat) shapes.I can name 3-D (solid) shapes.		

Classroom Snapshot			
Examples	Questions		
"I can name triangles, squares,	Show a collections of two-dimensional		
circles, rectangles, and hexagons."	three-dimensional shapes. Ask		
	students to sort the objects into the		
"I can name cubes, cones, cylinders and spheres."	categories "Two-Dimensional" or "Three- Dimensional."		
and spheres.	Thee-Dimensional.		
Adapted from Darke County Schools			
Grade K Common Core Math			
Ohio Department of Education Model Curriculum Instructional Strat	0		
Manipulatives used for shape identification actually have three dimensions			
two-dimensional or "flat" and typical three-dimensional shapes as "solid." Students will identify two-dimensional shapes that form surfaces on			
three-dimensional objects. Students need to focus on noticing two and three	e dimensions, not on the words two-dimensional and three-dimensional.		
Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 20	015		
Connections Across Standards			
Identify and describe measurable attributes (K.MD.1).			
Directly compare two objects with a measurable attribute (K.MD.2).			
Classify objects into given categories (K.MD.3).			
Pre-K (Prior Grade Standard)	1.G.2 (Future Grade Standard)		
Compare two-dimensional shapes, in different sizes and orientations,	Compose two-dimensional shapes (rectangles, squares, trapezoids, triangles, half aircles, and quarter aircles) or three dimensional		
using informal language.	triangles, half-circles, and quarter-circles) or three-dimensional shapes (cubes, right rectangular prisms, right circular cones, and right		
	circular cylinders) to create a composite shape, and compose new		
	shapes from the composite shape. (Note: Students do not need to		
	learn formal names such as "right rectangular prism.")		



K.G.4 that de parts, and other attributes.	5	Common Misconceptions One of the most common misconceptions in geometry is the belief that orientation is tied to shape. A student may see the first of the figures below as a triangle, but claim to not know the name of the second.	Academic Vocabulary/Language circle rectangle hexagon triangle square cube cylinder cone sphere roll stack slide vertices two-dimensional three-dimensional Tier 2 compare analyze describe
Learning Targets	I can describe the parts of a 2-D shape (flat) I can compare the parts of a 2-D shape. I can describe the parts of a 3-D shape (solid I can compare the parts of a 3-D shape.		

Ouestions

different

different

Have each child select two 2-D shapes and

share with the group one way the two

shapes are alike and one way they are

Have each child select 3-D shapes and

share with the group one way the two

shapes are alike and one way they are

Examples

"When I compare a square and a triangle, I notice that number of vertices are different and the number of sides are different."

"When I compare a cylinder and a cone, I notice they both have circle ends but the cylinder has two of them."

Adapted from Darke County Schools Grade K Common Core Math

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Use shapes collected from students to begin the investigation into basic properties and characteristics of two- and three-dimensional shapes. Have students analyze and compare each shape with other objects in the classroom and describe the similarities and differences between the shapes. Ask students to describe the shapes while the teacher records key descriptive words in common student language. Students need to use the word flat to describe two-dimensional shapes and the word solid to describe three-dimensional shapes.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards	
Identify and describe shapes (K.G.1-3).	
Identify and describe measurable attributes (K.MD.1).	
Directly compare two objects with a measurable attribute (K.MD.2).	
Classify objects into given categories (K.MD.3).	
Pre-K (Prior Grade Standard)	1.G.2 (Future Grade Standard)
Compare two-dimensional shapes, in different sizes and orientations,	Compose two-dimensional shapes (rectangles, squares, trapezoids,
using informal language.	triangles, half-circles, and quarter-circles) or three-dimensional
	shapes (cubes, right rectangular prisms, right circular cones, and right
	circular cylinders) to create a composite shape, and compose new
	shapes from the composite shape. (Note: Students do not need to
	learn formal names such as "right rectangular prism.")



K.G.5 s b	Model shapes in the world by building hapes from components e.g., sticks and clay balls and drawing shapes. tial Understanding nent can be represented with models.	Common Misconceptions Students may create 2D shapes when be asked to use 3D materials such as sticks, clay balls, etc. thus creating a 3D shape. Work with students to identify how 2D and 3D shapes are similar and different to develop an understanding of the attributes of 2D and 3D shapes.	Academic Vocabulary/Language round rectangle side square straight triangle Tier 2 analyze compare create compose
Learning Targets	I can make and draw 2-D (flat) shapes. I can make and draw 3-D (solid) shapes.		

Classroom Snapshot		
Examples	Questions	
"When given toothpicks and marshmallows,	Draw a triangle.	
I can build a cube."		
"When given clay, I can build a triangle."	Draw a rectangle.	
Adapted from Darke County Schools		
Ohio Department of Education Model Curriculum Instructional	Strategies and Resources	
The teacher and students orally describe and name the shapes. Studen	nts draw a shape and build it using materials regularly kept in the classroom	
such as construction paper, clay, wooden sticks or straws.		
Ohio's New Learning Standards Mathematics Kindergarten Model Curricu	lum 2015	
Connections Across Standards		
Identify and describe shapes (K.G.1-3).		
Identify and describe measurable attributes (K.MD.1).		
Directly compare two objects with a measurable attribute (K.MD.2).		
Classify objects into given categories (K.MD.3).		
Pre-K (Prior Grade Standard)	1.G.2 (Future Grade Standard)	
Create shapes during play by building, drawing, etc.	Compose two-dimensional shapes (rectangles, squares, trapezoids,	
	triangles, half-circles, and quarter-circles) or three-dimensional	
	shapes (cubes, right rectangular prisms, right circular cones, and right	
	circular cylinders) to create a composite shape, and compose new	
	shapes from the composite shape. (Note: Students do not need to	
	learn formal names such as "right rectangular prism.")	



K.G.6 Combine simple shapes to form larger shapes. Essential Understandings • Analyze, compare, create and compose shapes. • Shapes can be combined to form larger shapes.	Common Misconceptions Students may struggle to see a new shape from a composite shape. For example, a triangle and a square create a composite shape - pentagon. Students may see only the triangle and square not the pentagon. Students struggle to identify attributes of a shape that determines the shape name.	Academic Vocabulary/Language round rectangle side square straight triangle order Tier 2 analyze compare create compose
Learning Target I can put two shapes together to make mo	ore shapes that I can name.	

Example

"When I put two squares together, side by side, it looks just like a rectangle."

Question

Give the students 2 squares. Say: *Join these two squares to make a rectangle.* When the student is finished, ask: *How do you know that this new shape is a rectangle.*?

Adapted from Darke County Schools

Ohio Department of Education Model Curriculum Instructional Strategies and Resources

Have students compose (build) a larger shape using only smaller shapes that have the same size and shape. The sides of the smaller shapes should touch and there should be no gaps or overlaps within the larger shape. For example, use one-inch squares to build a larger square with no gaps or overlaps. Have students also use different shapes to form a larger shape where the sides of the smaller shapes are touching and there are no gaps or overlaps. Ask students to describe the larger shape and the shapes that formed it.

Ohio's New Learning Standards Mathematics Kindergarten Model Curriculum 2015

Connections Across Standards Identify and describe shapes (K.G.1-3). Identify and describe measurable attributes (K.MD.1). Directly compare two objects with a measurable attribute (K.MD.2). Classify objects into given categories (K.MD.3).	
Pre-K (Prior Grade Standard)	1.G.2 (Future Grade Standard)
Combine simple shapes to form larger shapes.	Compose two-dimensional shapes (rectangles, squares, trapezoids, triangles, half-circles, and quarter-circles) or three-dimensional shapes (cubes, right rectangular prisms, right circular cones, and right circular cylinders) to create a composite shape, and compose new shapes from the composite shape. (Note: Students do not need to learn formal names such as "right rectangular prism.")